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## Mathematical Sciences: MMSC4 <br> LESSON 11

UNIT STANDARD: 7449
Topic: Budgeting, Interest, Inflation and exchange rate

## By the end of this lesson, you should be able to:

- Calculate interest for both simple and compound investments.
- Determine and use the exchange rates correctly.
- Plan a budget based on income.


## 1. INTRODUCTION

- Budgeting is the process of creating a plan to spend your money. This spending plan is called a budget. Creating this spending plan allows you to determine in advance whether you will have enough money to do the things you need to do or would like to do.
- A budget is defined as a plan or estimate of the amount of money needed for cost of living or to be used for a specific purpose. An example of budget is how much a family spends on all expenses in a month. An example of budget is how much a person plans on spending on a new bed.
- Budgets are of three types -- balanced budget, surplus budget and deficit budget.
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2. Simple interest is calculated on the principal, or original, amount of a loan. Compound interest is calculated on the principal amount and also on the accumulated interest of previous periods, and can thus be regarded as "interest on interest.
Simple interest is only paid on principal, while compound interest is paid on the principal plus all of the interest that has previously been earned

## Simple Interest and Compound Interest

- What is the difference between simple interest and compound interest?
- Simple interest: Interest is earned only on the principal amount.
- Compound interest: Interest is earned on both the principal and accumulated interest of prior periods.

Compound vs Simple Interest
$8 \%$ per year for 40 Years

-FV (Simple Interest) - FV (Compound Interest)
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Simple Interest Formula,

$$
S I=\frac{P R T}{100}
$$

Where SI is the Simple interest
$P$ is the principal amount invested
$R$ is the rate (\%)
T is the time or period of the investment
Therefore, Amount will be,

$$
\begin{gathered}
\mathbf{A}=\mathbf{P}(\mathbf{1}+\mathbf{i t}) \\
\mathbf{A}=\mathbf{I}+\mathbf{P}
\end{gathered}
$$

Where I is Interest

## Compound Interest Formula,

$$
\mathbf{A}=\mathbf{P}(\mathbf{1}+\mathbf{i})^{\mathbf{t}}
$$

## Example 1

Faith invested R1500 to Esteem consult bank and he agreed to terminate the investment after 3 years at 12\% p.a. simple interest.
Calculate the interest of Faith's investment and total amount of the investment.

## Solution

$$
\begin{gathered}
S I=\frac{P R T}{100} \\
S I=\frac{1500 * 12 * 3}{100} \\
\text { SI }=\frac{54000}{100} \\
\text { SI }=\text { R540 }
\end{gathered}
$$

Therefore,

$$
\begin{gathered}
\mathrm{A}=\mathrm{R} 540+\mathrm{R} 1500 \\
\mathrm{~A}=\mathrm{R} 2040
\end{gathered}
$$

## Example 2

Lerato borrows R8000 from Esteem Consult for 5 years at 10\% interest compounded annually, what is the total amount Lerato needs to pay to Esteem Consult ?

## Solution

$$
\begin{gathered}
A=P(1+i)^{t} \\
A=8000(1+10 \%)^{5} \\
A=8000\left(1+\frac{10}{100}\right)^{5} \\
A=8000(1+0.1)^{5} \\
A=8000(1.1)^{5} \\
A=R 12884.08
\end{gathered}
$$

3. Inflation: is a sustained increase in the general price level of goods and services in an economy over a period of time.

South Atrica: Inflation rats from 1984 to 2024 (compared to the previous year)


1 Mand:

## Example

The population of a city in January 1960 was 30000 .The population is growing by $1.98 \%$ every year

Determine what the population of the city was in January 1971, if the growth remained constant.

## SOLUTION

$$
\begin{gathered}
A=P(1+i)^{t} \\
P=30000 \\
\mathbf{i}=\frac{1.98}{100} \\
t=1971-1960 \\
t=11 \\
A=30000\left(1+\frac{1.98}{100}\right)^{11} \\
A=37220.85 \\
\text { Population }=37220
\end{gathered}
$$

(a)
4. Exchange rate is the price of one currency in terms of another currency.

Description: Exchange rates can be either fixed or floating. Fixed exchange rates are decided by central banks of a country whereas floating exchange rates are decided by the mechanism of market demand and supply.
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## EXAMPLE,

| American dollar | 0,144 | 6,945 |
| :--- | :--- | :--- |
| Australian dollar | 0,144 | 6,948 |
| Botswana pula | 0,954 | 1,048 |
| British pound | 0,090 | 11,107 |
| Euro | 0,105 | 9,565 |
| Hong Kong dollar | 1,122 | 0,891 |
| Japanese yen | 11,905 | 0,084 |
| Singapore dollar | 0,183 | 5,453 |
| Thai baht | 4,386 | 0,228 |

Use above table to determine
a. Israel is travelling to United State and he wants to buy $\$ 1$ 200. How much Israel will pay in Rands?
b. A British tourist travelling to South Africa is quoted R54 000 for a two weeks holiday. What will this cost him in British pounds?

## SOLUTION

a. $1200 \times 6.945=\operatorname{R8} 334$
b. $54000 \times 0.090=£ 4860$

## ACTIVITY 1

Calculate the simple interest earned on investing R5 000 at $8,5 \%$ interest p.a. for 5 years.

Calculate the total amount owed if R12 500 is borrowed at $12,5 \%$ p.a. simple interest for 30 months.

How long will it take to double an amount of money invested at $12,5 \%$ p.a. $S!$ ?

## ACTIVITY 2

Find the compound interest earned on investing R2 600 at
$7 \%$ p.a. CI for 4 years.

How much money would you have at the end of 5 years, if you invested R15 070 at 9,75\% p.a. Cl?

## ACTIVITY 3

Use the following exchange rates to answer the questions:
$\$ 1: R 7,05$; $£ 1:$ R11,35 and $€ 1:$ R9,92.
You found the following prices for a Mini Cooper S on the Internet. Calculate each value in rands and decide which is the cheapest option if you were to buy the car. (Overseas prices include transport and import costs to SA.)
a) USA - $\$ 21850$
b) Germany - $€ 20950$
c) RSA - R206 100
d) UK - $£ 17580$

